

INNOVATIVE GRAPHS VIA E_J -NEIGHBORHOODS RISING FROM IDEALS

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ABSTRACT

Neighborhoods systems is an important tool for graphs in view of topological. So, in this paper, we establish new types of eight neighborhoods via the notion of set-ideal and E_j -neighborhoods from vertices of any graph. Then, the accuracy measures and boundary regions of these approximations are calculated. We explore novel types of j-lower (resp. j-upper) approximations are obtained and some algorithms are introduced. Finally, we give a real-life problem which is related to our methods.

Keywords Neighborhood Systems · Rough Sets · Graph Topology · j-Accuracy Measure

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